

CAPILLARY BREAKUP TO DETERMINE THE EXTENSIONAL PROPERTIES OF POLYMERIC FLUIDS

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Consultation, Testing, and Instrumentation for Polymeric Materials

Introduction



- Industrial processing conditions always have some form of extensional deformation
 - Pumping, Filling, Spreading, Extrusion, Spinning and Ink-jets
- Biological Fluids often exposed to extensional flows
- Standard characterization techniques all shear
- Some work on extensional deformation
 - Filament Stretching Extensional Rheometer (FiSER) and similar
 - Rheometrix RME
 - RFX Opposed Jet
- Some techniques give pseudo-extensional properties
 - Capillary Rheometer
 - Fiber line tension
 - Falling ball
 - etc

References

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Capillary Breakup Extensional Rheometer (CaBER™)



- Original concept by Entov and co-workers
- Fluid sets time scale
 - “Instantaneous” stretch in first case
 - Drainage governed by fluid
 - viscosity, elasticity, relaxation time, surface tension, effective extensional viscosity etc.
 - Gives measure of rheological parameters
 - Also measure of industrially relevant characteristic values
 - break-up time, stringiness etc.
- Analogous to “thumb-and-forefinger” test
 - sliding fingers gives how “slimy”
 - separating gives how “sticky”



[References](#)

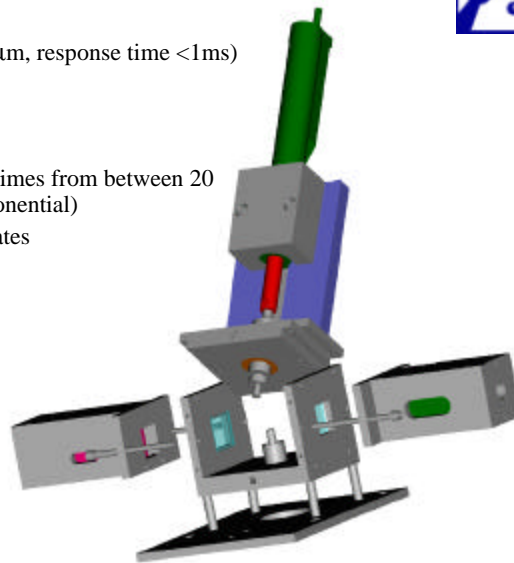
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The CaBER™



- Laser Micrometer (resolution 5 μm , response time <1ms)
- Drive system:
 - Manual
 - Solenoid
 - Linear motor drive (stretch times from between 20 ms and >100s, linear or exponential)
- 6 mm diameter stainless steel plates
 - interchangeable
- Oven:
 - Low temperature to 120 °C
 - High temperature to 300 °C (in development)
- Force
- Camera
- Patent Pending



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CaBER™ - “Simple” Fluids

Constitutive Model	Form of Solution	Parameters found from regression to data
Newtonian, $\mathbf{t} = \mathbf{h}\dot{\mathbf{g}}$	$D_{mid}(t) = 0.142 (s/h_s)(t_c - t)$	$t_c, s/h_s$
Power-Law Fluids $\mathbf{t} = K\dot{\mathbf{g}}^n$	$D_{mid}(t) = 2^{1-n} (0.142)(s/K)(t_c - t)^n$	$t_c, s/K, n$
Upper Convected Maxwell $\mathbf{t} + \mathbf{1}t_{(t)} = \mathbf{h}\dot{\mathbf{g}}$	$D_{mid}(t) = D_0 (GD_0/s)^{1/3} \exp(-t/3I_c)$	$I_c, G/s$

- Newtonian
 - dynamics of the drainage of fluid column and rupture of the liquid bridge governed by viscous and elastic properties of fluid
- Viscoelasticity
 - rapid initial viscous-dominated phase, then intermediate time -scale where the filament drainage is governed by surface tension and elasticity

References

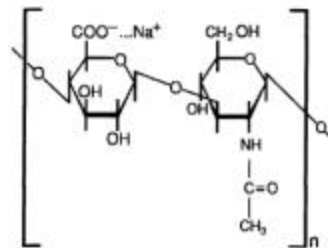
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Test Fluids

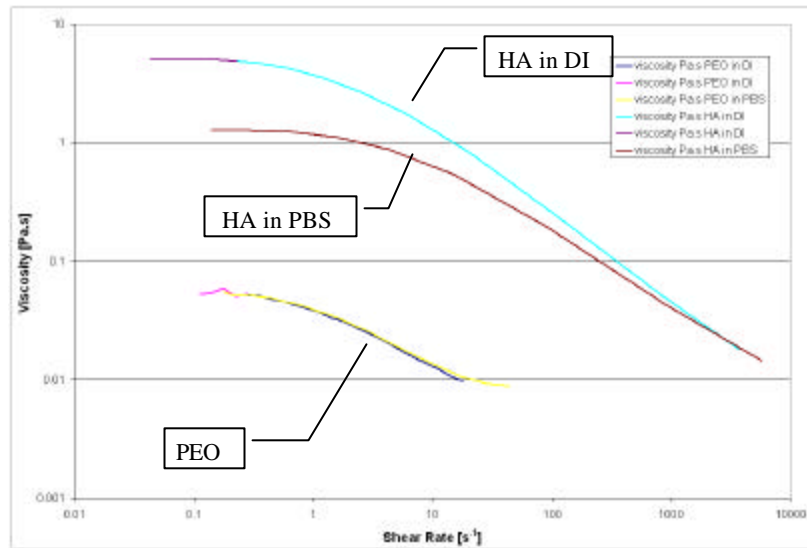
- Sodium Hyaluronate (HA)
 - 0.5 wt% in water at different salt concentrations (physiological in joint is ~0.3wt%)
 - Polysaccharide of sodium glucuronate and N-acetyl glucosamine
 - Molecular weight 1.68×10^6 g/mol
 - Known to associate in solution
- PEO from Scientific Polymer Products
 - 0.5 wt% in water at different salt concentrations
 - molecular weight 2.5×10^6 g/mol
- Cannon Instruments Newtonian Viscosity Standard N350
- Deionised water (DI) and Dulbecco’s Phosphate Buffered Saline (PBS)
- Shear Rheology performed on TA Instruments AR1000N using a cone and plate geometry
- All experiments performed at $25 \text{ }^\circ\text{C} \pm 2 \text{ }^\circ\text{C}$



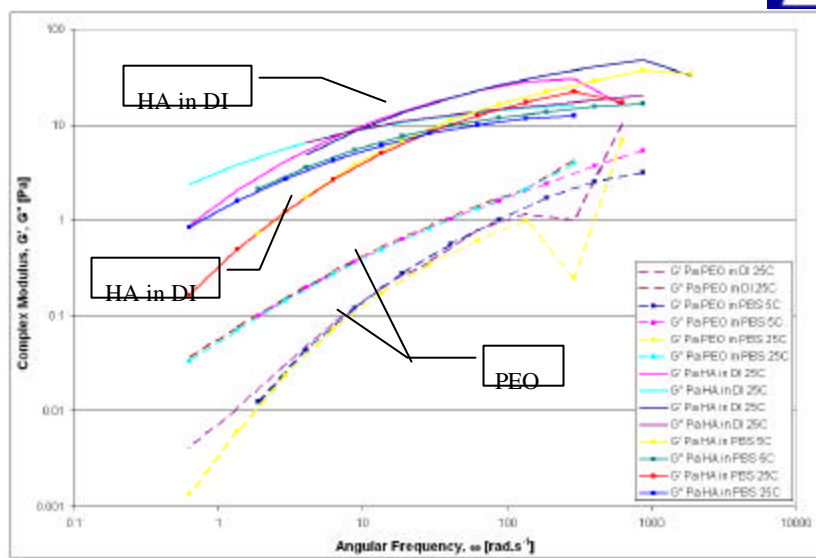
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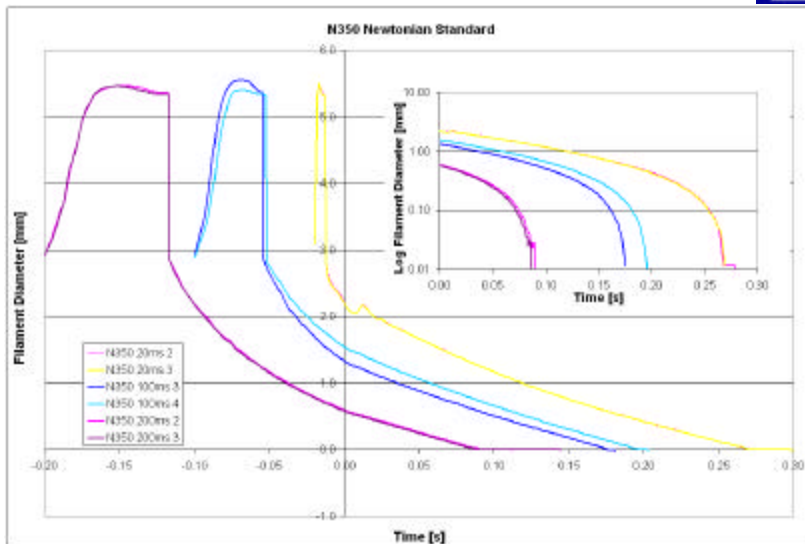
Shear Rheology (Steady)



Shear Rheology (Dynamic)



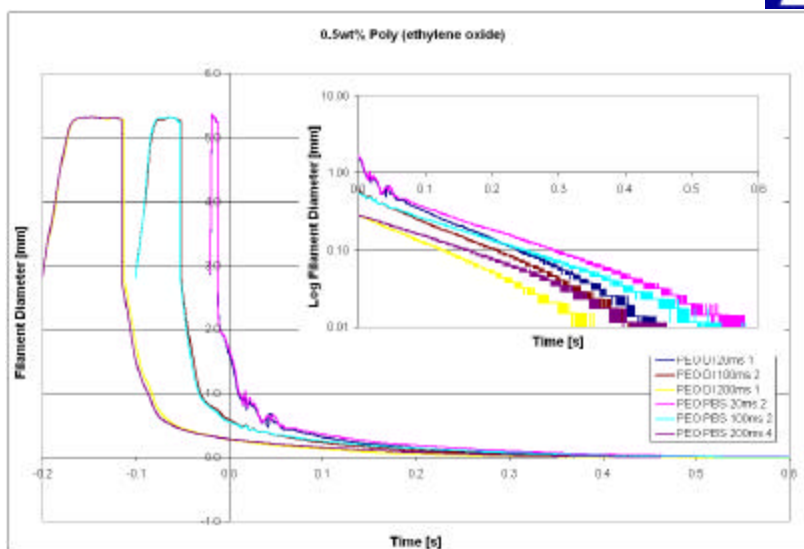
N350 Newtonian Standard Fluid



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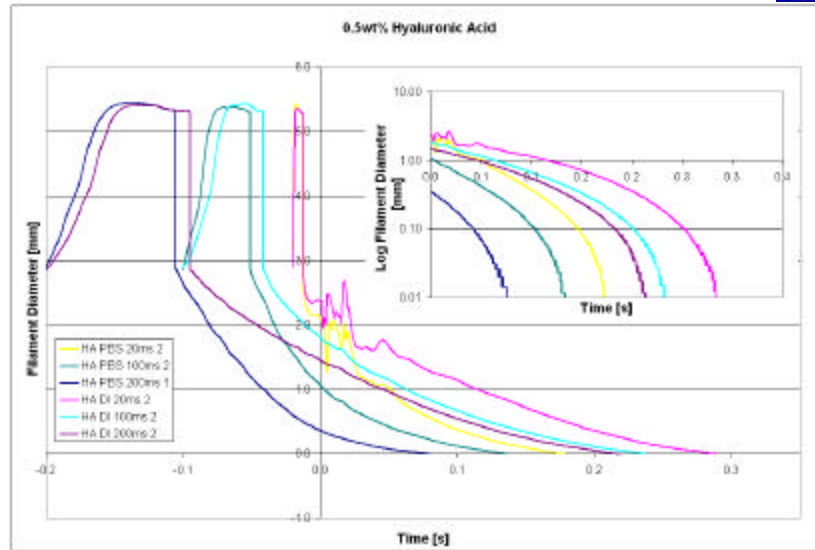
pEO Elastic Fluid



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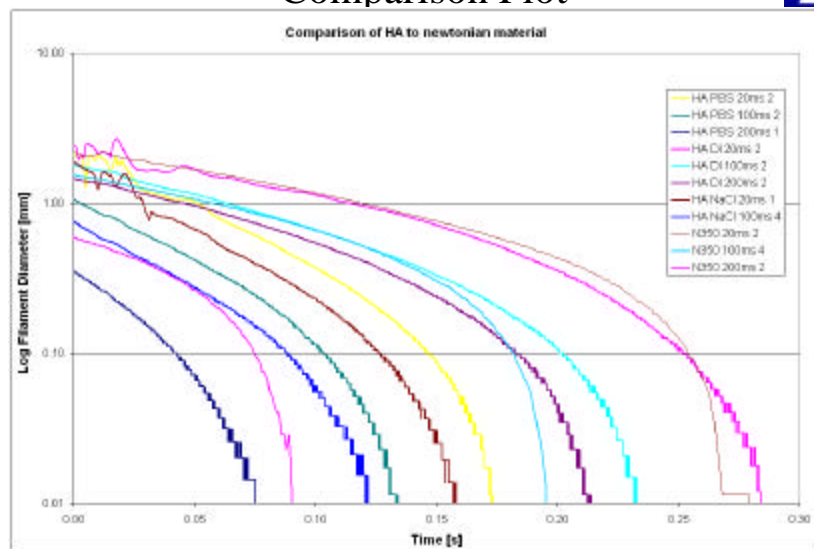
Hyaluronic Acid



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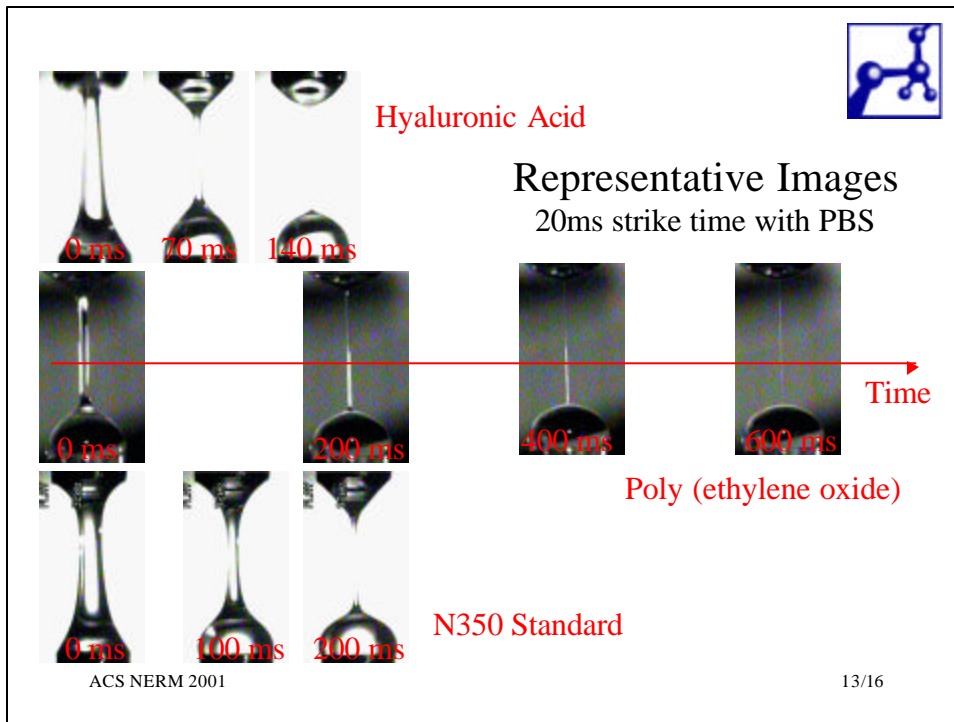
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Comparison Plot




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Calculated rheological parameters



Fluid	Determined Viscosity [Pa.s]	Determined Relaxation Time [s]	Actual Viscosity [Pa.s] ³	Actual relaxation time [s] ³
N350	0.77 ¹	N/A	0.75 ²	N/A
0.5 wt% PEO in DI	N/A	0.040	0.05	<0.05
0.5wt% PEO in PBS	N/A	0.045	0.05	<0.05
0.5 wt% HA in DI	N/A	N/A	5.1	1
0.5 wt% HA in PBS	N/A	N/A	1.3	0.3

¹ Assuming Surface Tension of 36 mN.m of Poly(butene)
² From Cannon Fluid Specifications @ 25 °C
³ From Shear Rheology

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Summary



- Demonstrated an instrument capable of studying capillary breakup of simple and complex fluids
 - Leads directly to information on the extensional properties of fluids
 - Fluid sets timescale
 - Complementary to shear data
- Presented data for three different fluids
 - Model Newtonian
 - Elastic
 - Associative (note rates)

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Conclusions



- Physiological fluids increasingly studied
 - Hyaluronic acid is clearly not a simple Newtonian liquid, nor is it a simple elastic fluid.
 - Shear rheology suggests a polymeric solution
 - Extensional rheology clearly indicates more complex
 - Salt subtle effect on PEO, strong effect on HA
 - Disruption of water “cage” around PEO?
 - Implication is PEO is less flexible in salt
 - Charge Screening on HA (but no effect on character of flow)
 - HA more flexible in salt or smaller “molecules”
 - HA is strike rate dependent – perhaps evidence for association
 - Rate dependence due to elasticity of fluid
 - “Shear Thinning” for HA suggest structure

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CaBER™ - “Complex” Fluids

- Complex fluids
- A balance of forces on the fluid filament governs the evolution in the midpoint profile of the liquid bridge
- Allows derivation of an “apparent” extensional viscosity

$$3h_s \underbrace{\left(-\frac{2}{D_m} \frac{dD_m}{dt} \right)}_{\text{Viscous Stress}} = 3h \dot{\epsilon} = \underbrace{\frac{4F_z}{\pi D_m^2}}_{\text{Tensile Stress}} - \underbrace{\left[\frac{t_z - t_{rr}}{2} \right]}_{\text{Elastic/Non-Newtonian Stress}} - \underbrace{\frac{2s}{D_m}}_{\text{Capillary Pressure}}$$

$$\bar{\Pi}_{app}(\dot{\epsilon}) = \frac{2s/D_{mid}(t)}{\left\{ -\frac{2}{D_{mid}} \frac{dD_{mid}}{dt} \right\}} = \frac{s}{\frac{dD_{mid}}{dt}}$$

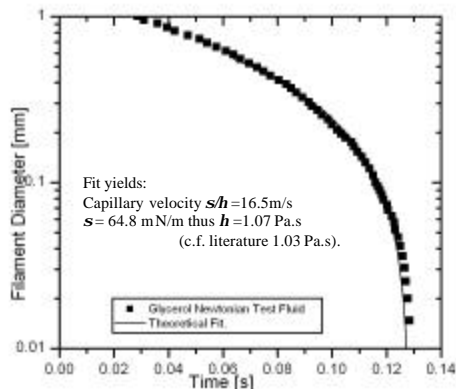
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Example Data

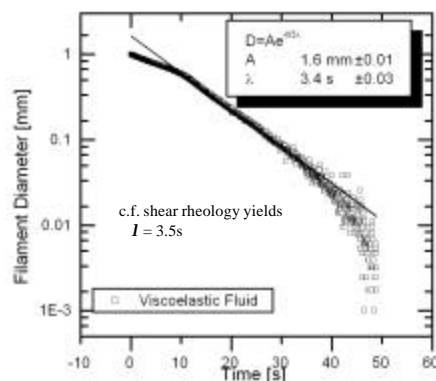
$$D_{mid}(t) = D_1 - \frac{(2X(t)-1)s}{3h_s} t$$



Glycerol

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$$D_{mid}(t) = \frac{GD_0}{s} \exp(-t/3I_c)$$



0.025 wt% 2.5×10^6 Mw
PS in Styrene oligomer

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